**QUICK FATIGUE TOOL FOR MATLAB®**

# Appendices

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# Version Information

**Documentation revision: 10 [14/12/2017]**

**Concurrent code release: 6.11-10**

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# Appendix I. Fatigue analysis techniques

## A1.1 Background

Quick Fatigue Tool is capable of assessing the fatigue life of entire FEA models. This is achieved by reading the stress tensor at each analysis item (node, integration point or centroid) and performing a damage calculation at each location in the model.

Before the analysis begins, the FEA definitions are combined with the load history to form a scaled time history of stresses at each location in the model. This is known as a *Scale and Combine* analysis.

The stresses at each location must be considered in multiple directions in order to account for multiaxial stress states. The plane which experiences the largest stress is isolated, and the load signal is cycle counted to obtain the stress amplitudes, so that a damage calculation can be performed.

The damage of each cycle in the loading is summed for each analysis item. The item with the largest damage is identified as the *worst* item and the fatigue life is quoted at this location. During the damage calculation process, the endurance limit may be modified to account for the effect of microscopic plasticity at the crack tip.

This section provides a concise description of how the code achieves the above steps.

## A1.2 Combining FEA stresses with a loading

FE models usually comprise of multiple analysis steps, each representing a distinct load configuration for which the stress state is solved. Provided these stresses are elastic, each loading state may be combined with its respective load history to create a single scaled, combined loading, as depicted in Figure A1.1.



Figure A1.1: Illustration of a scale and combine loading

## A1.3 Critical plane search algorithm

Critical plane analysis is a widely used engineering methodology to determine multiaxial fatigue damage where the most damaging stresses are not readily apparent [1] [2] [3] [4]. It has been argued that fatigue criteria cased on critical plane methods are the most effective [5].

Quick Fatigue Tool uses a critical plane approach based on a combination of work by R. Rabb and Luca Susmel.

The stress tensor history at each node is transformed onto a series of planes according to Figure A1.1 [6].



Figure A1.1: Tensor transformation

The rotated tensor, , is calculated from the original tensor by Equation A1.1.

|  |  |  |
| --- | --- | --- |
|  |  | [A1.1] |

Where is the transformation matrix given by Equation A1.2.

|  |  |  |
| --- | --- | --- |
|  |  | [A1.2] |

The angles and correspond to the cylindrical coordinate system described by Figure A1.1. The rotated tensor is split into one normal and two shear components:

|  |  |  |
| --- | --- | --- |
|  |  | [A1.3] |

Depending on the algorithm, the normal and/or shear stresses are cycle counted in order to calculate fatigue damage.

## A1.4 Rainflow cycle counting

The rainflow counting method is used for the analysis of fatigue loadings which reduces a spectrum of variable amplitude stresses into a matrix of simple stress reversals. The advantage of such a method is that it allows for efficient summation of fatigue damage using Miner’s rule [7] [8]. The original rainflow method was devised by Tatsuo Endo and M. Matsuishi [9]. However, as of 2008, several counting algorithms are available [10] [11] [12] [13].

Quick Fatigue Tool uses a custom-written algorithm which follows a similar logic to that of the original rainflow methodology. Cycles are counted on the basis of comparing adjacent pairs of stress ranges and removing these points from the loading until no more cycles are closed.

The cycle counting strategy is as follows:

1. Convert the load history into a sequence of peaks and valleys (no intermediate values between inflection points)
2. Re-arrange the history so that the absolute maximum stress is at the start of the signal. Perform the same re-arrangement on the indexes so that the true position of the data points is retained
3. Remove leading and trailing tails (identical values forming flat paths on either side of the load history
4. Remove plateaus (adjacent points with the same value) which can arise from step 2
   1. If the plateau lies between two diametrically opposed inflection points (a peak-valley pair), remove all plateaued points
   2. If the plateau lies between two diametrically similar inflection points (two peaks or two valleys), remove only the current plateau
5. For the current pair of history points, compare the current stress range to the previous stress range
   1. If the current stress range exceeds the previous stress range, count a cycle and remove the previous stress range from the loading
6. Repeat step 5 until no more cycles can be extracted
7. Move to the next pair of history points and repeat steps 5 and 6 until all cycles have been removed from the loading
8. Check for unmatched half cycles and add these to the cycle matrix until there is no more history data

The algorithm does not consider the nonlinear relationship between stress and strain. Therefore, the effect of cyclic hysteresis and material memory is not included. Since changes in the mean stress due to plasticity are ignored, the performance of the cycle counting algorithm will degrade as fatigue lives decrease below one million repeats.

The method described above is implemented from version 6.6 onwards. The previous version of the cycle counting algorithm can be enabled from the environment file. Values of 1.0 and 2.0 correspond to the old and new versions, respectively.

*Environment file usage:*

|  |  |
| --- | --- |
| *Variable* | *Value* |
| **rainflowAlgorithm** | **{**1.0 | 2.0**}** |

## A1.5 Treatment of the endurance limit

### A1.5.1 Overview

The endurance limit is the region on the stress-life curve where fatigue damage does not occur, irrespective of the number of applied stress cycles [14]. Ferrous and titanium alloys exhibit a distinct limit below which the fatigue life is observed to be infinite. However, other nonferrous alloys such as aluminium and copper do not have a distinct limit and will eventually fail regardless of the applied stress amplitude. The concept of the endurance limit is illustrated by the plateau in Figure A1.3.



Figure A1.3: Representative Stress-Life curves for steel and aluminium, indicating the presence (and lack thereof) an endurance limit stress below which no fatigue damage occurs.

**Image courtesy of Andrew Dressel (Wikimedia Commons: CC-BY-SA-3.0)**

### A1.5.2 Enforcement of the endurance limit

Quick Fatigue Tool may ignore fatigue damage for cycles below the endurance limit depending on the setting of the following environment variable:

*Environment file usage:*

|  |  |
| --- | --- |
| *Variable* | *Value* |
| **ndEndurance** | **{**0.0 | 1.0 | 2.0**}** |

If **ndEndurance** is set to 0.0, Quick Fatigue Tool determines from the table below whether to account for the endurance limit based on the material behavior defined in the material. Values of 1.0 and 2.0 disable or enable treatment of the endurance limit, respectively.

|  |  |
| --- | --- |
| **Material Behavior** | **Ignore damage below endurance limit?** |
| Aluminium alloys | NO |
| All other material classifications | YES |

Guidance on defining material behavior can be found in Section 5.9 in the document *Quick Fatigue Tool User Guide*.

### A1.5.3 Endurance limit of non-ferrous metals

Due to the difficulties associated with testing specimens to very long lives, it is not always feasible to determine the exact endurance limit of the material. Furthermore, for some nonferrous metals as well as very strong steels, the stress-life curve is observed to continuously decrease as far as the test data are available. As a result, materials are often considered to cross into infinite life at a pre-determined limit (usually cycles), beyond which it is usually safe to assume that no damage will occur. Thus, if the material is classified as *Other* in the material definition, the endurance limit is enforced.

### A1.5.4 The “bouncing endurance limit”

Investigations have shown that cycles below the endurance limit can result in fatigue damage from otherwise non-damaging cycles [15]. This phenomenon can be explained by considering a cycle just above the endurance limit. Since the cycle is large enough to cause fatigue damage, it acts to open the crack tip resulting in a very small plastic zone ahead of the crack. This microscopic plasticity temporarily reduces the fatigue strength of the specimen at the crack tip, until the crack propagates through the plastic zone. The phenomenon of a “bouncing endurance limit” has been investigated in considerable detail [16] [17] [18] [19] [20].

This behavior is modelled in Quick Fatigue Tool such that the fatigue limit is reduced by a factor, , if the current cycle is damaging and only applies when enforcement of the endurance limit is enabled.

*Environment file usage:*

|  |  |
| --- | --- |
| *Variable* | *Value* |
| **ndEndurance** | **{**0.0[[1]](#footnote-1) | 1.0 |2.0**}** |
| **modifyEnduranceLimit** | **{**0.0 | 1.0**}** |
| **enduranceScaleFactor** |  |

Over the course of the next consecutive non-damaging cycles, the fatigue limit is linearly incremented back to its original value. By default, and [21].

*Environment file usage:*

|  |  |
| --- | --- |
| *Variable* | *Value* |
| **cyclesToRecover** |  |

If any subsequent cycle exceeds the fatigue limit, the limit will be scaled back to a factor of of its original value and the recovery process will start from the beginning.

# Appendix II. Materials data generation

## A2.1 Background

Despite extensive efforts over years in characterizing the fatigue behavior of metals, obtaining fatigue materials data is often time consuming and expensive. Therefore, it is important to be aware of methods which are capable of producing reasonable estimates of material data based on readily available information.

Quick Fatigue Tool offers several approximation algorithms which can estimate the fatigue materials data:

1. Uniform Law (Bäumel-Seeger)
2. Universal Slopes (Manson)
3. Modified Universal Slopes (Muralidharan)
4. 90/50 Rule

## A2.2 Bäumel-Seeger Method

The Bäumel-Seeger method approximates the fatigue materials data as follows [22] [23] [24]:

|  |  |  |
| --- | --- | --- |
| **Fatigue Property** | **Plain/Alloy Steel** | **Aluminium** |
|  |  |  |
| Fatigue strength coefficient |  |  |
|  |  |  |
| Fatigue strength exponent |  |  |
|  |  |  |
| Fatigue ductility coefficient |  |  |
|  |  |  |
| Fatigue ductility exponent |  |  |
|  |  |  |
| Cyclic strain hardening coefficient |  |  |
|  |  |  |
| Cyclic strain hardening exponent |  |  |

## A2.3 Manson

The Manson method approximates the fatigue materials data as follows [25]:

|  |  |  |  |
| --- | --- | --- | --- |
| **Fatigue Property** | **Plain/Alloy Steel** | **Aluminium** | **Other** |
|  |  |  |  |
| Fatigue strength coefficient |  |  |  |
|  |  |  |  |
| Fatigue strength exponent |  |  |  |
|  |  |  |  |
| Fatigue ductility coefficient |  |  |  |
|  |  |  |  |
| Fatigue ductility exponent |  |  |  |
|  |  |  |  |
| Cyclic strain hardening coefficient |  |  |  |
|  |  |  |  |
| Cyclic strain hardening exponent |  |  |  |

## A2.4 Modified Manson

The Modified Manson method approximates the fatigue materials data as follows [26]:

|  |  |  |  |
| --- | --- | --- | --- |
| **Fatigue Property** | **Plain/Alloy Steel** | **Aluminium** | **Other** |
|  |  |  |  |
| Fatigue strength coefficient |  |  |  |
|  |  |  |  |
| Fatigue strength exponent |  |  |  |
|  |  |  |  |
| Fatigue ductility coefficient |  |  |  |
|  |  |  |  |
| Fatigue ductility exponent |  |  |  |
|  |  |  |  |
| Cyclic strain hardening coefficient |  |  |  |
|  |  |  |  |
| Cyclic strain hardening exponent |  |  |  |

## A2.5 90/50 Rule

The *90/50* rule is an informal approximation of the stress-life relationship. It assumes the following two points on the endurance curve if only the ultimate tensile strength is known:

|  |  |
| --- | --- |
| **Life ()** | **Stress (S)** |
| 1000 | 0.9 |
|  | 0.5 |

Basquin’s exponent is then the gradient of the straight line defined by the above two points when plotted on log-log axes:

|  |  |  |
| --- | --- | --- |
|  |  | [A2.1] |

where is the constant amplitude endurance limit. Note that the value of depends only on the endurance limit and not on the ultimate tensile strength.

The relationship between the ultimate tensile strength and the fatigue limit becomes increasingly nonlinear with increasing ultimate tensile strength. Therefore, if the UTS exceeds 1000MPa, the endurance limit stress is fixed to 500MPa and Equation A2.2 is used to approximate Basquin’s exponent:

|  |  |  |
| --- | --- | --- |
|  |  | [A2.2] |

If the stress-life relationship is given by Equation A2.3, then the value of the tensile fatigue strength coefficient, , may be derived using Equation A2.4 which assumes that .

|  |  |  |
| --- | --- | --- |
|  |  | [A2.3] |
|  |  |  |
|  |  | [A2.4] |

If cycles, then the stress life equation is given by Equation A2.5:

|  |  |  |
| --- | --- | --- |
|  |  | [A2.5] |

In general, the stress-life relationship is given by Equation A2.6:

|  |  |  |
| --- | --- | --- |
|  |  | [A2.6] |

# Appendix III. Gauge fatigue toolbox

## A3.1 Background

### A3.1.1 Overview

The Gauge Fatigue Toolbox is a set of MATLAB apps which facilitate the analysis of measured strain data. The following apps are included:

* *Multiaxial Gauge Fatigue*
* *Rosette Analysis*
* *Virtual Strain Gauge*

In addition to the above, the toolbox also includes *Mohr Solver* for calculating principal stresses and strains for a given stress tensor.

The toolbox is located in *Application\_Files\toolbox*. To install the app, double click on the *.mlappinstall* file. The app appears in the *Apps* tab of the MATLAB ribbon UI.

### A3.1.2 Gauge conventions

The strain gauge is defined as a three-armed rosette and is placed relative to the reference coordinate system shown in Figure A3.1.



Figure A3.1: Gauge orientation relative to the reference axis. Rosette arms are separated by angles α, β and γ

The user must define the gauge orientation relative to the reference coordinate system. If the Image Processing Toolbox is installed, the GUI contains an  icon which displays the active gauge orientation. The orientation can be defined in three ways:

1. Rectangular
2. Delta
3. User-defined

**Rectangular**

The rectangular orientation is the special case where the strains , and from the rosette arms A, B and C, respectively,coincide with the reference axes.

|  |  |  |
| --- | --- | --- |
|  |  | [A3.1] |

The principal strains, and , are readily calculated from the gauge strains:

|  |  |  |
| --- | --- | --- |
|  |  | [A3.2] |

**Delta**

The delta orientation is the special case where the rosette arms are separated by degrees and rosette arm A is rotated degrees counter-clockwise from the positive reference direction.

The principal strains are readily calculated from the gauge strains:

|  |  |  |
| --- | --- | --- |
|  |  | [A3.3] |

**User-defined**

User-defined gauge orientations allow the user to specify the angles α, β and γ directly. The reference strains are then solved as a system of linear equations.

|  |  |  |
| --- | --- | --- |
|  |  | [A3.4] |

The principal strains are calculated from the reference strains:

|  |  |  |
| --- | --- | --- |
|  |  | [A3.5] |

**Stress determination**

Assuming an elastic relationship, the principal stresses are determined from the principal strains:

|  |  |  |
| --- | --- | --- |
|  |  | [A3.6] |

where is Young’s Modulus and is Poisson’s ratio. The reference stresses , and may be determined from Equation A3.6 by substituting and with and , respectively.

**Reference orientations**

The reference orientation is the angle between the reference axes and the principal/shear axes. The orientations are calculated as follows:

|  |  |  |
| --- | --- | --- |
|  |  | [A3.7] |

where is the angle between the reference axes and the principal axes, and is the angle between the reference axes and the direction of maximum shear stress.

### A3.1.3 Strain units

The *Multiaxial Gauge Fatigue* and *Uniaxial Strain-Life* applications allow the user to select between strain [] and microstrain []. The *Rosette Analysis* and *Virtual Strain Gauge* applications both assume microstrain as the input units.

## A3.2 Multiaxial Gauge Fatigue

Multiaxial Gauge Fatigue is a strain-life analysis application which takes measured strain gauge data as the fatigue loading input. The application GUI is shown in Figure A3.2.

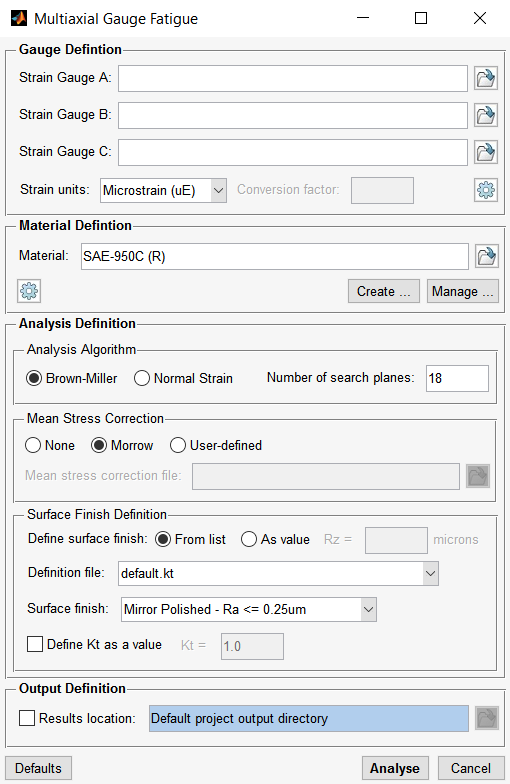


Figure A3.2: Multiaxial Gauge Fatigue GUI

### A3.2.1 Gauge Definition

By default, the gauge is assumed to be orientated in a rectangular fashion, i.e. , and . The gauge orientation can be modified by selecting the  button. This displays the gauge orientation dialogue shown in Figure A3.3.

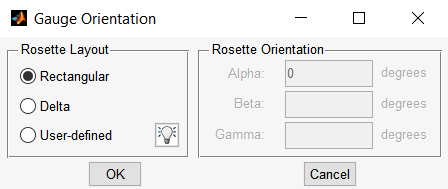


Figure A3.3: Gauge orientation dialogue

The gauge input is defined as a text file containing the measured strain history from its respective rosette arm. Absolute (full) and relative paths may be used. If no path is specified, the current working directory will be searched. The file extension must be included.

If the sample rate is not the same for all three gauges, an optional time history may be included for each gauge. The data file is formatted as follows:

|  |  |  |
| --- | --- | --- |
| Strain history | Time history (optional) |  |
|  |  | ← First strain point |
|  |  |  |
| . | . |  |
| . | . |  |
|  |  | ← Last strain point |

The data can be formatted as or , where is the number of strain samples. if no time history is specified and if a time history is specified.

If time histories are not specified, Quick Fatigue Tool assumes that the lapsed time between samples is equal. If the three signals contain the same number of samples, the phase will be preserved. If the strain histories are not the same length, zeros will be added to the end of the signals where applicable so that they all have the same number of sample points.

If the histories contain a different number of samples, and/or the lapsed time between measurements is not constant, the phase between the signals will be lost if time points are not specified, and inaccurate fatigue results may be obtained. When time histories are defined alongside the strain measurements, Quick Fatigue Tool interpolates the signals so that all three gauges contain measurements at the exact same time points. This ensures that the phase between the signals is preserved.

Time points do not have to be specified for all three gauges. Gauges which do not have time points will be assumed to be increasing monotonically through time:

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Strain |  |  |  |  |
| Time |  |  |  |  |

Time points do not have to be specified for every sample point. Missing time points will be interpolated automatically. When using time points, the first point must always be zero, and at least the first and last points must be defined.

The user should exercise caution when using time points. The underlying assumption remains that the strain measurements were obtained at identical points in time. The correction applied by Quick Fatigue Tool is intended for signals with small measurement delay. If the time points between the three gauges differ greatly, the resulting strain history may suffer from aliasing. This happens because of interpolating linearly a strain history which varies nonlinearly.

The default gauge units are microstrain []. User-defined units may be specified with a conversion factor such that:

|  |  |  |
| --- | --- | --- |
|  |  | [A3.8] |

### A3.2.2 Material definition

The material is selected either by browsing for an existing material (\*.mat) file, or by creating a new material with the Material Manager application. Absolute (full) or relative paths may be used. The file extension does not have to be included. For more information on defining material data, consult Section 5 of the document *Quick Fatigue Tool User Guide*.

Strain-life analysis requires the fatigue ductility (Coffin-Manson) parameters: The fatigue ductility coefficient () and the fatigue ductility exponent ().

Additional options relating to the material behavior are accessed by selecting **Options…** from the Material Definition region of the user interface. The options are shown in Figure A3.4.

**Include out-of-plane strains**

Rosette strain gauges can only detect plane strain and the analysis ignores out-of-plane strains by default. The assumption is that the thickness of the specimen is sufficient to constrain out-of-plane displacements, and that through-thickness strains would not cause fatigue damage. Selecting this option will enable calculation of the out-of-plane principal strain according to Equation A3.7.

|  |  |  |
| --- | --- | --- |
|  |  | [A3.9] |

This calculation assumes a constant section Poisson’s ratio and should only be used in cases where such an estimation is valid.

**Ignore damage below endurance limit**

Most steels exhibit a clearly defined knee-point, below which fatigue is not observed. In such cases, selecting this option will ignore cycles whose stress amplitude is below the pre-determined fatigue limit. The fatigue limit is defined as the strain amplitude which would result in a fatigue life equal to the material’s constant amplitude endurance limit.

Materials such as aluminium do not exhibit a fatigue limit. For these materials, this option should not be selected.

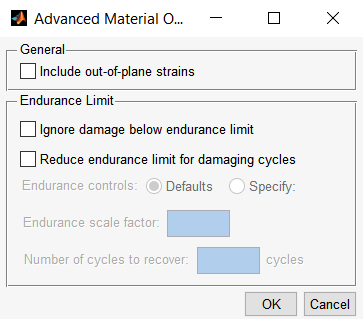


Figure A3.4: Material options

**Reduce endurance limit for damaging cycles**

If the user selects to ignore damage below the endurance limit, this option can be additionally selected which will automatically reduce the endurance limit in response to a damaging cycle. The resulting behavior is that previously non-damaging cycles (below the original fatigue limit), will become damaging.

By default, the endurance limit is scaled by a factor of , and recovers linearly to its original value over the course of non-damaging cycles. If any cycle exceeds its instantaneous fatigue limit during the recovery process, the endurance limit is reset to the scaled value. The user may change these defaults by selecting the **Specify:** radio button and manually entering the values of the endurance limit scale factor and the number of cycles to recover.

### A3.2.3 Analysis definition

The gauge fatigue analysis can be run with either the Brown-Miller or the Principal Strain algorithm. These two algorithms work in a similar fashion to the Stress-based Brown-Miller and Normal Stress algorithms described in Sections 6.2 and 6.3 of the document *Quick Fatigue Tool User Guide*, respectively. Strains are resolved onto a series of planes and fatigue damage is calculated on the plane which experiences the largest combination of normal and shear strain (Brown-Miller) or the largest normal strain (Principal Strain).

The number of search planes can be selected from the GUI. The use of 18 search planes is found to be sufficient in most cases. Increasing the number of search panes drastically increases the analysis time.

### A3.2.4 Mean Stress Correction

The analysis can be run without mean stress correction, or with either the Morrow correction or a user-defined mean stress correction file.

The Morrow mean stress correction modifies the elastic region of the strain-life equation:

|  |  |  |
| --- | --- | --- |
|  |  | [A3.10] |

The mean stress has a more significant effect on the material’s endurance at higher lives. The Morrow correction subtracts the mean stress from the fatigue strength coefficient.

User-defined mean stress correction can be performed by selecting a mean stress correction (\*.msc) file. Absolute (full) and relative paths may be used. If no path is specified, the current working directory will be searched. The file extension must be included. User-defined mean stress corrections are discussed in Section 7.9 of the document *Quick Fatigue Tool User Guide*.

To perform mean stress correction, the true stresses must be obtained from the measured strain history. If mean stress correction is specified, the program converts the principal strain history into principal stresses before the analysis, and uses the stress and strain for the critical plane analysis.

The relationship between true stress and strain is assumed to obey a multilinear cyclic strain-hardening law. This is accomplished with the Ramberg-Osgood relationship for cyclic stress and strain:

|  |  |  |
| --- | --- | --- |
|  |  | [A3.11] |

Where and is the true strain and stress range, respectively. Since the true strain is used, elastic-plastic correction such as Neuber’s rule is not required. The effect of material memory is considered whereby if a cycle is closed, the material stress-strain response continues as though the reversal had not occurred. This behavior is illustrated by Figure A3.5. This allows for the effect of ratcheting to be considered.

The current approach for calculating the stresses is limited by the assumption that the strain history is already cyclically stable. Therefore, the analysis does not make additional correction for the effect of kinematic hardening. Depending on the hardening characteristics of the material, fatigue results obtained from the Multiaxial Gauge Fatigue application may be on the non-conservative side. In such cases, additional care and consideration should be taken by the user.

### A3.2.5 Surface Finish Definition

Surface finish is specified either directly or by surface finish type. The effect of surface finish is discussed in Section 4.3 of the document *Quick Fatigue Tool User Guide*.

### A3.2.6 Output Definition

In addition to a fatigue analysis summary, the Multiaxial Gauge Fatigue application writes the following history output:

|  |  |
| --- | --- |
| **ST, NT, DPP, DP, LP** | Maximum shear strain, maximum normal strain, damage parameter, damage and life as a function of plane angle |
|  |  |
| **HD** | Mean stress and strain amplitude for each cycle in the load history |
|  |  |
| **CN, CS** | Normal and resultant shear strain history on the critical plane |
|  |  |
| **EST** | Principal tensor history. Includes the principal stress if mean stress correction is used |

The following MATLAB figures are produced:

|  |  |
| --- | --- |
| **CN + CS** | Normal and shear strain history on the critical plane |
| **CPS** | Normal strain and resultant shear stress vs. plane angle |
| **CSS*n*** | Cyclic stress-strain curves for maximum, middle and minimum principal stress-strain histories |
| **DP** | Damage vs. angle |
| **DPP** | Damage parameter vs. angle |
| **LP** | Life vs. angle |
| **PS** | Time-correlated principal stresses |
| **PE** | Time-correlated principal strains |
| **RHIST** | Rainflow cycle histogram |

## A3.3 Rosette Analysis

The Rosette Analysis GUI is shown in Figure A3.6.



Figure A3.6: Rosette Analysis GUI

The purpose of this application is to process data from a strain gauge to convert it into principal stresses and strains. Strain data is specified for the three gauge arms. The strain is defined in units of microstrain [].

Input is specified either by selecting an ASCII text file containing the strain gauge history, or by defining the history directly in the edit field. Histories defined directly must follow MATLAB syntax of a vector, e.g. [2000, -2000].

The gauge orientation must be defined. A rectangular orientation corresponds to , and , whereas a delta layout would be defined as , and . However, any user gauge orientation may be specified.

The user may request the output in terms of principal strain or principal stress. Additionally, the reference orientations and stress/strain may be requested. The reference orientations and stress/strain are given by Equation A3.7 and Equation A3.4, respectively.

All available output variables and their identifiers are listed below.

|  |  |
| --- | --- |
| **PE1** | Maximum principal strain |
|  |  |
| **PE2** | Minimum principal strain |
|  |  |
| **E12(MAX)** | Maximum shear strain |
|  |  |
| **E11(R)** | Normal strain in reference -direction |
|  |  |
| **E22(R)** | Normal strain in reference -direction |
|  |  |
| **E12(R)** | Shear strain in reference -direction |
|  |  |
| **PS1** | Maximum principal stress |
|  |  |
| **PS2** | Minimum principal stress |
|  |  |
| **S12(MAX)** | Maximum shear stress |
|  |  |
| **S11(R)** | Normal stress in reference -direction |
|  |  |
| **S22(R)** | Normal stress in reference -direction |
|  |  |
| **S12(R)** | Normal stress in reference -direction |
|  |  |
| **φD** | Angle between principal and reference axes |
|  |  |
| **φS** | Angle between maximum shear and reference axes |

Output stress, strain and angle units are , and , respectively.

## A3.4 Virtual Strain Gauge

The Virtual Strain Gauge GUI is shown in Figure A3.7.



Figure A3.7: Virtual Strain Gauge GUI

The purpose of this application is to mimic the output of a virtual strain gauge in response to a strain tensor. The strain tensor represents the response of the structure onto which the virtual gauge would be adhered. This tool is useful for determining the theoretical response of a rosette strain gauge at a specific orientation.

Input is specified by selecting an ASCII text file containing the strain gauge data. The text file has the following format:

|  |  |  |  |
| --- | --- | --- | --- |
|  |  |  |  |
| . | . | . | ← First strain point |
| . | . | . |  |
|  |  |  | ← Last strain point |

In the above example, the strain components are defined by three separate columns representing the reference , and shear directions, respectively. However, the strain data may be defined by rows or columns, provided that the user specified this with the *Read data from* radio buttons. The strain is defined in units of microstrain [].

The process of converting the input data in strain gauge histories is describes in Section 4.9 of the document *Quick Fatigue Tool User Guide*.

## A3.5 Mohr Solver

The Mohr Solver GUI is shown in Figure A3.8.



Figure A3.8: Mohr’s Circle Solver GUI

The principal stresses are given by Equation A3.12.

|  |  |  |
| --- | --- | --- |
|  |  | [A3.12] |

The maximum shear stresses are given by Equation A3.13.

|  |  |  |
| --- | --- | --- |
|  |  | [A3.13] |

The maximum normal stresses are given by Equation A3.14.

|  |  |  |
| --- | --- | --- |
|  |  | [A3.14] |

## A3.6 Uniaxial Strain-Life

Uniaxial Strain-Life is a strain-life analysis application which takes a stress or strain history as the fatigue loading input. The application GUI is shown in Figure A3.9.

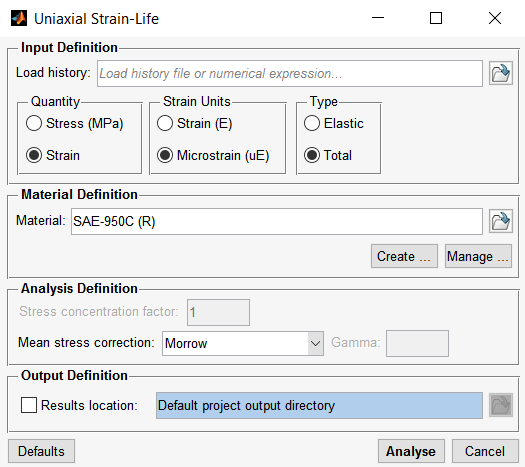


Figure A3.9: Uniaxial Strain-Life GUI

### A3.6.1 Input definition

The input is specified as a stress or strain history. The stress is assumed to be elastic, and the strain can be elastic or inelastic.

The application converts the input history into the inelastic stress and strain, which is then rainflow cycle counted so that the strain amplitude can be obtained. The elastic stress is converted into inelastic stress and strain using the Ramberg-Osgood nonlinear elastic cyclic strain hardening relationship (Equation A.15) with Neuber’s correction (Equation A.16).

|  |  |  |
| --- | --- | --- |
|  |  | [A.15] |
|  |  |  |
|  |  | [A.16] |

The user of the Ramberg-Osgood model is described in the table below.

|  |  |  |
| --- | --- | --- |
| **Input** | **Ramberg-Osgood** | **Neuber’s Rule?** |
| Elastic stress () | Solve for and | Yes |
| Elastic strain () | Convert to  Solve for and | Yes |
| Inelastic strain () | Solve for | No |

Input is specified either by selecting an ASCII text file containing the history data, or by defining the history directly in the edit field. Histories defined directly must follow MATLAB syntax of a vector, e.g. [2000, -2000].

### A3.6.2 Material definition

The material is selected either by browsing for an existing material (\*.mat) file, or by creating a new material with the Material Manager application. Absolute (full) or relative paths may be used. The file extension does not have to be included. For more information on defining material data, consult Section 5 of the document *Quick Fatigue Tool User Guide*.

### A3.6.3 Analysis definition

The fatigue analysis uses the Strain-Life relationship in Equation A.17.

|  |  |  |
| --- | --- | --- |
|  |  | [A.17] |

where is the uniaxial strain amplitude.

A stress concentration factor can be specified, which scales the elastic stress and strain in the Neuber correction.

The Morrow, Smith-Watson-Topper and Walker mean stress corrections are available. For more information on mean stress correction, consult Section 7 of the document *Quick Fatigue Tool User Guide*.

### A3.6.4 Output definition

In addition to a fatigue analysis summary, the Uniaxial Strain-Life application writes the following history output:

|  |  |
| --- | --- |
| **LH** | Input load history before and after gating |
|  |  |
| **HD** | Mean strain and strain amplitude for each cycle in the load history |
|  |  |
| **CSS** | Inelastic cyclic stress-strain history |

# Appendix IV. List of supported elements for surface detection

The surface detection algorithm described in Section 4.5.3 “Specifying the analysis region” of the document *Quick Fatigue Tool User Guide* supports the following Abaqus elements.

## A4.1 3D continuum hexahedron (brick) elements

C3D8, C3D8H, C3D8I, C3D8IH, C3D8R, C3D8RH, C3D8S, C3D8HS, C3D20, C3D20H, C3D20R, C3D20RH, C3D8T, C3DHT, C3D8RT, C3D8RHT, C3D20T, C3D20HT, C3D20RT, C3D20RHT.

## A4.2 3D continuum hexahedron (brick) elements for solid composite sections

C3D8C3, C3D8IC3, C3D8RC3, C3D8HC3, C3D8RHC3, C3D8IHC3, C3D20C3, C3D20HC3, C3D20RC3, C3D20RHC3.

## A4.3 3D continuum tetrahedral elements

C3D4, C3D4H, C3D10, C3D10H, C3D10HS, C3D10M, C3D10MH, C3D4T, C3D10T, C3D10HT, C3D10MT, C3D10MHT.

## A4.4 3D continuum wedge (triangular prism) elements

C3D6, C3D6H, C3D15, C3D15H.

## A4.5 3D continuum pyramid elements

C3D5, C3D5H.

## A4.6 3D conventional triangular shell elements

STRI3, S3, S3R, S3RS, STRI65, S3T, S3RT.

## A4.7 3D conventional quadrilateral shell elements

S4, S4R, S4RS, S4RSW, S4R5, S8R, S8R5, S4T, S4RT, S8RT, S9R5(S).

## A4.8 General triangular membrane elements

M3D3, M3D6(S).

## A4.9 General quadrilateral membrane elements

M3D4, M3D4R, M3D8(S), M3D8R(S), M3D9(S), M3D9R(S).

## A4.10 3D continuum triangular shell elements

SC6R, SC6RT.

## A4.11 3D continuum hexahedral shell elements

SC8R, SC8RT

## A4.12 3D continuum solid hexahedral shell elements

CSS8

## A4.13 2D continuum triangular elements:

CPE3, CPE3H, CPE6, CPE6H, CPE6M, CPE6MH, CPS3, CPS6, CPS6M, CPEG3, CPEG3H, CPEG6, CPEG6H, CPEG6M, CPEG6MH.

## A4.14 2D continuum quadrilateral elements:

CPE4, CPE4H, CPE4I, CPE4IH, CPE4R, CPE4RH, CPE8, CPE8H, CPE8R, CPE8RH, CPS4, CPS4I, CPS4R, CPS8, CPS8R, CPEG4, CPEG4H, CPEG4RH, CPEG8, CPEG8H, CPEG8R, CPEG8RH.

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|  |  |
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1. If **ndEndurance** = 0.0, the “bouncing endurance limit” is enabled unless the material behaviour is aluminium, in which case damage below the endurance limit is always allowed. [↑](#footnote-ref-1)